Ss Alban and Stephen RC Infant and Nursery School written calculations policy

This policy outlines the progression through written strategies for addition, subtraction, multiplication and division in line with the new National Curriculum commencing September 2014. This policy will ensure consistency of approach, enabling children to progress stage by stage through models and representations they recognise from previous teaching, allowing for deeper conceptual understanding and fluency. As children move at the pace appropriate to them, teachers will be presenting strategies and equipment appropriate to children's level of understanding. However, it is expected that the majority of children in each class will be working at age-appropriate levels as set out in the National Curriculum 2014 and in line with school policy.

The importance of mental mathematics

While this policy focuses on written calculations in mathematics, we recognise the importance of the mental strategies and known facts that form the basis of all calculations. The following checklists outline the key skills and number facts that children are expected to develop throughout the school.

To add and subtract successfully, children should be able to:

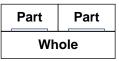
- recall all addition pairs to 9 + 9 and number bonds to 10
- recognise addition and subtraction as inverse operations
- add mentally a series of one digit numbers (e.g. 5 + 8 + 4)
- add and subtract multiples of 10 or 100 using the related addition fact and their knowledge of place value (e.g. 600 + 700, 160 70)
- partition 2 and 3 digit numbers into multiples of 100, 10 and 1 in different ways (e.g. partition 74 into 70 + 4 or 60 + 14)
- use estimation by rounding to check answers are reasonable

To multiply and divide successfully, children should be able to:

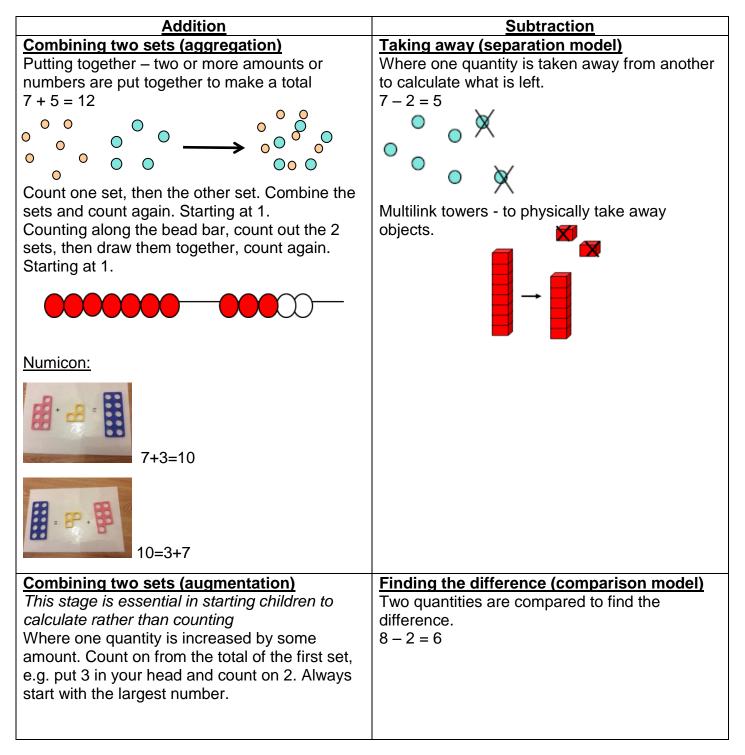
- add and subtract accurately and efficiently
- recall multiplication and division facts for 2, 3, 4, 5 and 10 times tables.
- use multiplication and division facts to estimate how many times one number divides into another etc.
- know the outcome of multiplying by 0 and by 1 and of dividing by 1
- understand the effect of multiplying and dividing whole numbers by 10, 100 and later 1000
- recognise factor pairs of numbers (e.g. that $15 = 3 \times 5$, or that $40 = 10 \times 4$) and increasingly able to recognise common factors
- derive other results from multiplication and division facts and multiplication and division by 10 or 100 (and later 1000)
- notice and recall with increasing fluency inverse facts
- partition numbers into 100s, 10s and 1s or multiple groupings
- understand how the principles of commutative, associative and distributive laws apply or do not apply to multiplication and division
- understand the effects of scaling by whole numbers or fractions
- investigate and learn rules for divisibility

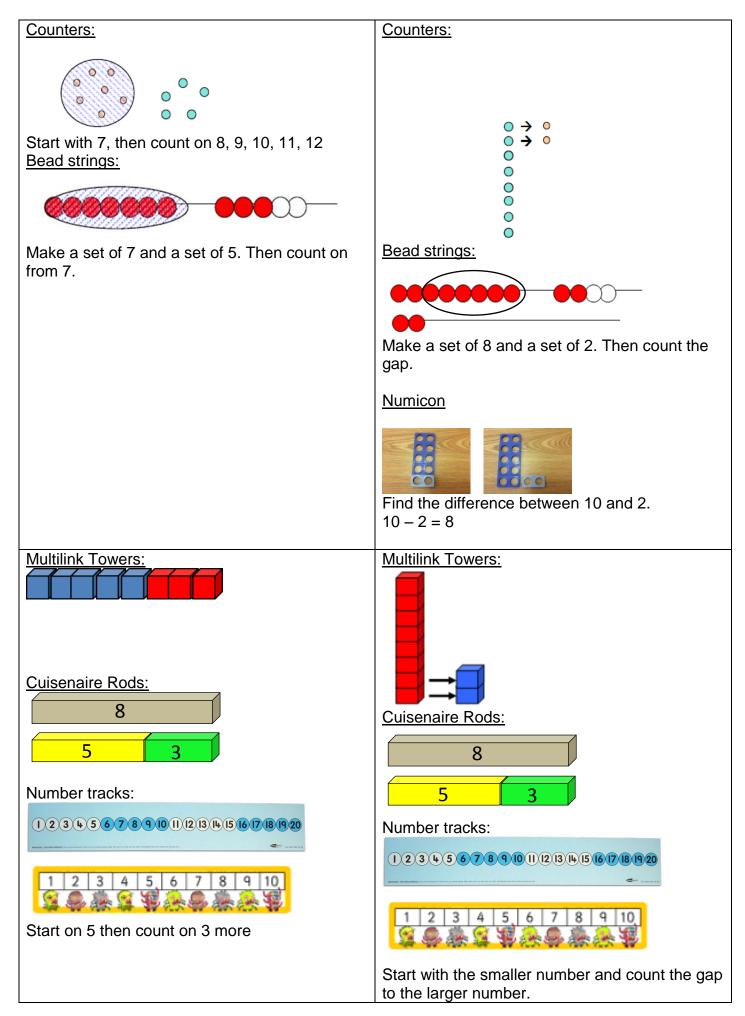
Progression in addition and subtraction

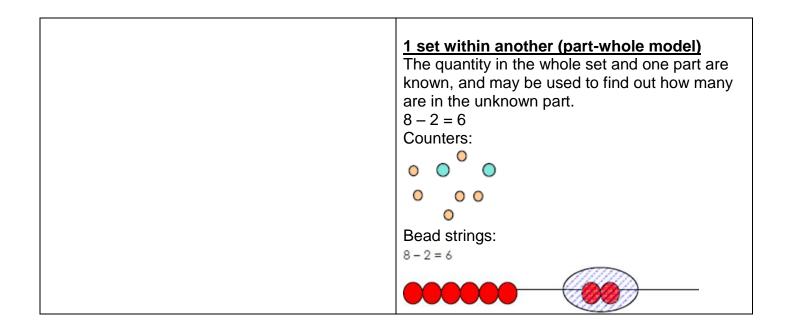
Addition and subtraction are connected.



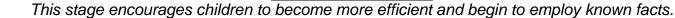
Addition names the whole in terms of the parts and subtraction names a missing part of the whole.



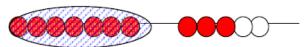




Bridging through 10s



Bead string:



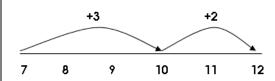
7 + 5 is decomposed / partitioned into 7 + 3 + 2. The bead string illustrates 'how many more to the next multiple of 10?' (children should identify how their number bonds are being applied) and then 'if we have used 3 of the 5 to get to 10, how many more do we need to add on? (ability to decompose/partition all numbers applied)

Number track:

123456789011231415678920

Steps can be recorded on a number track alongside the bead string, prior to transition to number line.

Number line

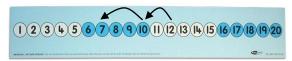


Bead string:



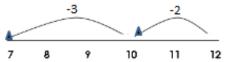
12 - 7 is decomposed / partitioned in 12 - 2 - 5. The bead string illustrates 'from 12 how many to the last/previous multiple of 10?' and then 'if we have used 2 of the 7 we need to subtract, how many more do we need to count back? (ability to decompose/partition all numbers applied)

Number Track:



Steps can be recorded on a number track alongside the bead string, prior to transition to number line.

Number Line:



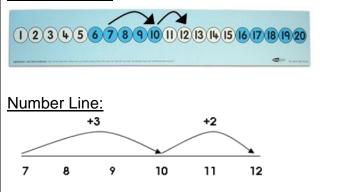
Counting up or 'Shop keepers' method

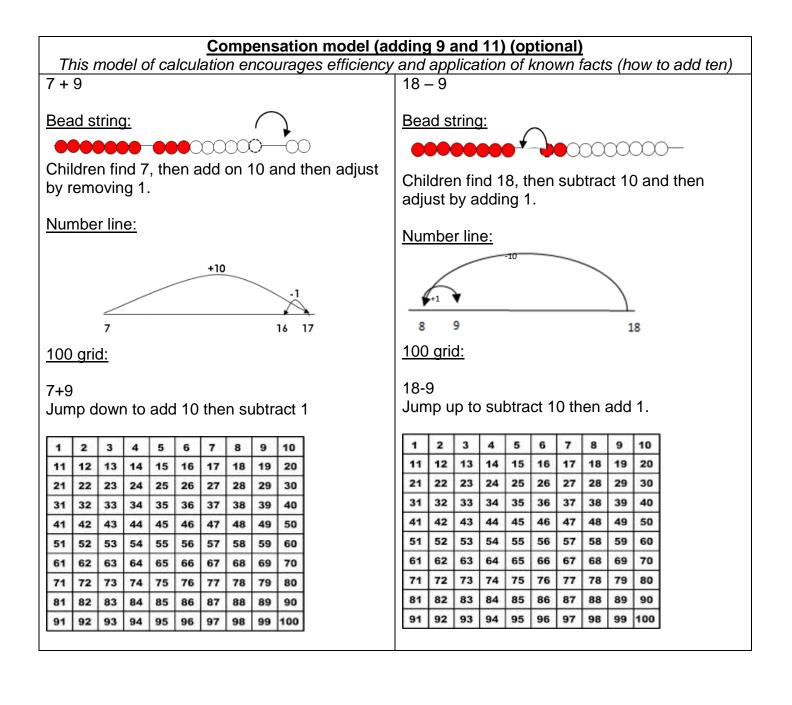
Bead string:



12 - 7 becomes 7 + 3 + 2. Starting from 7 on the bead string 'how many more to the next multiple of 10?' (children should recognise how their number bonds are being applied), 'how many more to get to 12?'.

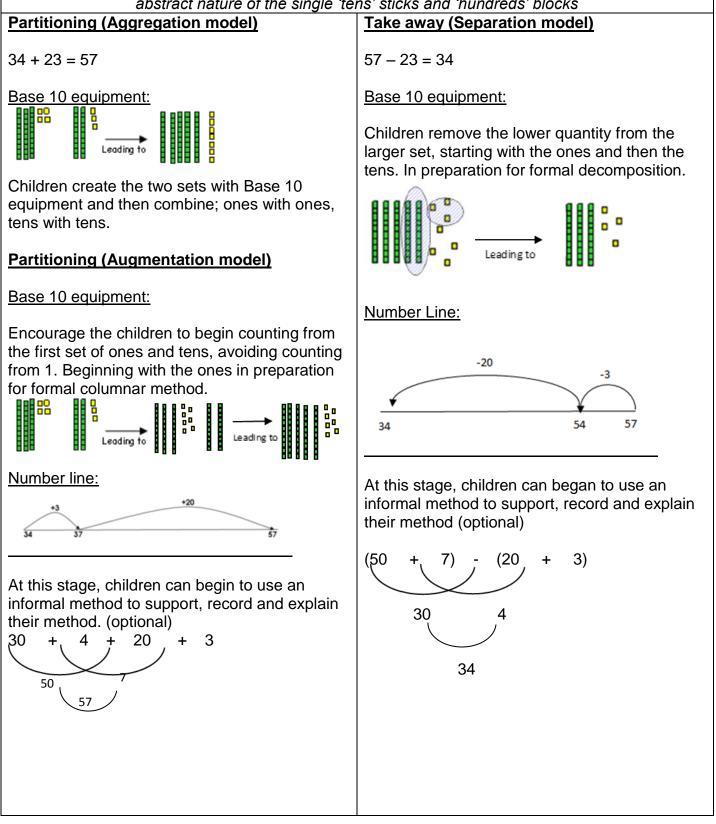
Number Track:





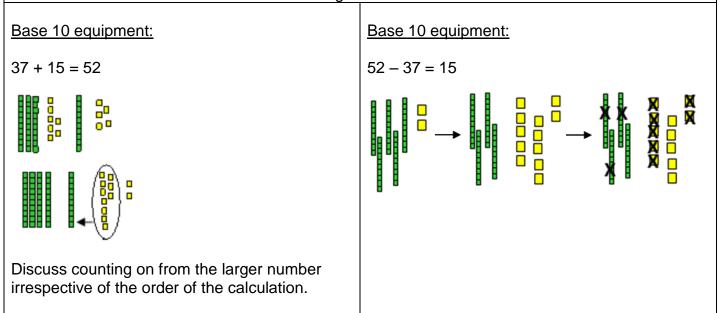
Working with larger numbers Tens and ones + tens and ones

Ensure that the children have been transitioned onto Base 10 equipment and understand the abstract nature of the single 'tens' sticks and 'hundreds' blocks



Bridging with larger numbers

Once secure in partitioning for addition, children begin to explore exchanging. What happens if the ones are greater than 10? Introduce the term 'exchange'. Using the Base 10 equipment, children exchange ten ones for a single tens rod, which is equivalent to crossing the tens boundary on the bead string or number line.



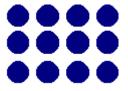
Gradation of difficulty- addition:	Gradation of difficulty- subtraction:
1. No exchange	1. No exchange
2. Extra digit in the answer	2. Fewer digits in the answer
3. Exchanging ones to tens	3. Exchanging tens for ones
4. Exchanging tens to hundreds	4. Exchanging hundreds for tens
5. Exchanging ones to tens and tens to hundreds	5. Exchanging hundreds to tens and tens to ones
6. More than two numbers in calculation	6. As 5 but with different number of digits
7. As 6 but with different number of digits	

Progression in Multiplication and Division

Multiplication and division are connected.

Both express the relationship between a number of equal parts and the whole.

Part	Part	Part	Part
Whole			



The following array, consisting of four columns and three rows, could be used to represent the number sentences: -

3 x 4 = 12,

- 4 x 3 =12,
- 3 + 3 + 3 + 3 = 12,

4 + 4 + 4 = 12.

And it is also a model for division

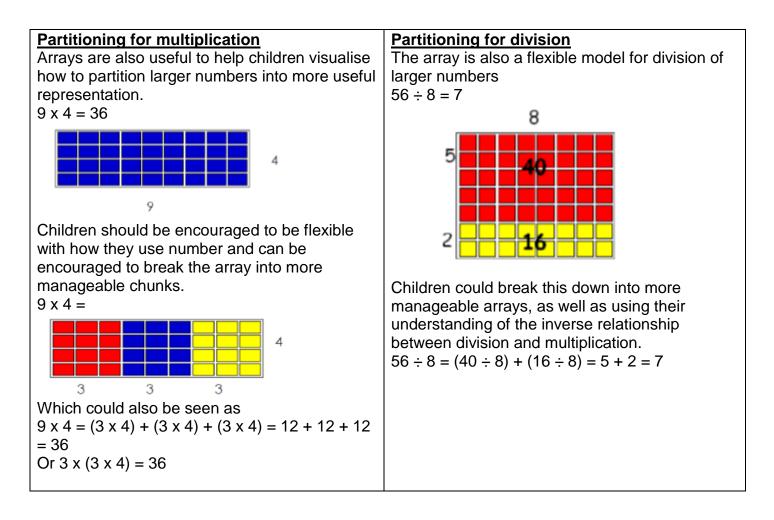
 $12 \div 4 = 3$

- $12 \div 3 = 4$
- 12 4 4 4 = 0
- 12 3 3 3 3 = 0

Multiplication	Division
Early experiences Children will have real, practical experiences of handling equal groups of objects and counting in 2s, 10s and 5s. Children work on practical problem solving activities involving equal sets or groups.	Children will understand equal groups and share objects out in play and problem solving. They will count in 2s, 10s and 5s.
Repeated addition (repeated aggregation) 3 times 5 is 5 + 5 + 5 = 15 or 5 lots of 3 or 5 x 3 Children learn that repeated addition can be shown on a number line. Children learn that repeated addition can be shown on a bead string.	Sharing equally 6 sweets get shared between 2 people. How many sweets do they each get? A bottle of fizzy drink shared equally between 4 glasses.
Numicon: Find 4 fives. $4 \times 5 = 20$	Grouping or repeated subtraction There are 6 sweets. How many people can have 2 sweets each? Mumicon: How many fives are there in 20? $20 \div 5 = 4$

Scaling This is an extension of augmentation in addition, except, with multiplication, we increase the quantity by a scale factor not by a fixed amount. For example, find a ribbon that is 4 times as long as the blue ribbon. Define 20 cm	Repeated subtraction using a bead string or number line 12 ÷ 3 = 4 The bead string helps children with interpreting division calculations, recognising that 12 ÷ 3 can be seen as 'how many 3s make 12?'
	Grouping involving remainders Children move onto calculations involving remainders. $13 \div 4 = 3 r1$
Commutativity Children learn that 3 x 5 has the same total as 5 x 3. This can also be shown on the number line. $3 \times 5 = 15$ $5 \times 3 = 15$	Or using a bead string see above. Children learn that division is not commutative and link this to subtraction.
<u>Arrays</u> Children learn to model a multiplication calculation using an array. This model supports their understanding of commutativity and the development of the grid in a written method. It also supports the finding of factors of a number.	Children learn to model a division calculation using an array. This model supports their understanding of the development of partitioning and the 'bus stop method' in a written method. This model also connects division to finding fractions of discrete quantities.

$\bigcirc \bigcirc $	$ \bigcirc \bigcirc$
Inverse operationsTrios can be used to model the 4 relatedmultiplication and division facts. Children learnto state the 4 related facts. $3 \times 4 = 12$ $4 \times 3 = 12$ 12	This can also be supported using arrays: e.g. 3 X ? = 12
12 ÷ 3 = 4 12 ÷ 4 = 3 Children use symbols to represent unknown numbers and complete equations using inverse operations. They use this strategy to calculate the missing numbers in calculations. $\Box x 5 = 20$ 3 x $\triangle = 18$ O x $\Box = 32$ 24 ÷ 2 = \Box 15 ÷ O = 3 \triangle ÷ 10 = 8	



Gradation of difficulty (short multiplication)	Gradation of difficulty (short division)
1. TO x O no exchange	1. TO ÷ O no exchange no remainder
2. TO x O extra digit in the answer	2. TO ÷ O no exchange with remainder
3. TO x O with exchange of ones into tens	3. TO ÷ O with exchange no remainder
4. HTO x O no exchange	4. TO \div O with exchange, with remainder
5. HTO x O with exchange of ones into tens	5. Zero in the quotient e.g. 816 ÷ 4 = 204
6. HTO x O with exchange of tens into hundreds	6. As 1-5 HTO ÷ O
7. HTO x O with exchange of ones into tens and	7. As 1-5 greater number of digits ÷ O
tens into hundreds	8. As 1-5 with a decimal dividend e.g. 7.5 \div 5 or
8. As 4-7 but with greater number digits x O	0.12 ÷ 3
	9. Where the divisor is a two digit numbers
	Dealing with remainders
	Remainders should be given as integers, but children need to be able to decide what to do after division, such as rounding up or down accordingly. e.g.: I have 62p. How many 8p sweets can I
	buy?
	 Apples are packed in boxes of 8. There

-
are 86 apples. How many boxes are needed?
Gradation of difficulty for expressing remainders
 Whole number remainder Remainder expressed as a fraction of the divisor Remainder expressed as a simplified fraction
4. Remainder expressed as a decimal